GradeMax

Pearson Edexcel

Mark Scheme (Results)

Summer 2023

Pearson Edexcel International Advanced Level In Pure Mathematics P2 (WMA12) Paper 01

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Summer 2023
Question Paper Log Number 72869
Publications Code WMA12_01_2306_MS
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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

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General Instructions for Marking

The total number of marks for the paper is 75.

Edexcel Mathematics mark schemes use the following types of marks:

'M' marks
These are marks given for a correct method or an attempt at a correct method. In Mechanics they are usually awarded for the application of some mechanical principle to produce an equation, e.g. resolving in a particular direction; taking moments about a point; applying a suvat equation; applying the conservation of momentum principle; etc.

The following criteria are usually applied to the equation.

To earn the M mark, the equation
(i) should have the correct number of terms
(ii) each term needs to be dimensionally correct

For example, in a moments equation, every term must be a 'force x distance' term or 'mass x distance', if we allow them to cancel 'g' s.

For a resolution, all terms that need to be resolved (multiplied by sin or cos) must be resolved to earn the M mark.

'M' marks are sometimes dependent (DM) on previous M marks having been earned, e.g. when two simultaneous equations have been set up by, for example, resolving in two directions and there is then an M mark for solving the equations to find a particular quantity – this M mark is often dependent on the two previous M marks having been earned.

'A' marks
These are dependent accuracy (or sometimes answer) marks and can only be awarded if the previous M mark has been earned. e.g. M0 A1 is impossible.

'B' marks
These are independent accuracy marks where there is no method (e.g. often given for a comment or for a graph).

A and B marks may be f.t. – follow through – marks.

General Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod means benefit of doubt
- ft means follow through
    - the symbol $\surd$ will be used for correct ft
- cao means correct answer only
- cso means correct solution only, i.e. there must be no errors in this part of the question to obtain this mark
- isw means ignore subsequent working

- awrt means answers which round to
- SC means special case
- oe means or equivalent (and appropriate)
- dep means dependent
- indep means independent
- dp means decimal places
- sf means significant figures
- * means the answer is printed on the question paper
- ⎡⎣ means the second mark is dependent on gaining the first mark

All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

Ignore wrong working or incorrect statements following a correct answer.

General Principles for Pure Mathematics Marking

(NB specific mark schemes may sometimes override these general principles)

Method mark for solving 3 term quadratic:

- Factorisation
  - o $(x^2 + bx + c) = (x + p)(x + q)$, where $|pq| = |c|$, leading to $x = ...$
  - o $(ax^2 + bx + c) = (mx + p)(nx + q)$, where $|pq| = |c|$ and $|mn| = |a|$, leading to $x = ...$
- Formula
  - o Attempt to use the correct formula (with values for *a*, *b*and *c*).
- Completing the square
  - o Solving $x^2 + bx + c = 0$: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0, \ q \neq 0$, leading to $x = ...$

Method marks for differentiation and integration:

- Differentiation
  - o Power of at least one term decreased by 1. ($x^n \to x^{n-1}$)
- Integration
  - o Power of at least one term increased by 1. ($x^n \to x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first. Normal marking procedure is as follows:

- Method mark for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.
- Where the formula is not quoted, the method mark can be gained by implication from correct working with values but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required. Most candidates do show working, but there are occasional awkward cases and if the mark scheme does not cover this, please contact your team leader for advice.

Question Number	Scheme	Marks
1	$h = 0.2$	B1
	$\frac{1}{2}\times"0.2"\times\left[9.2+8.6+2(8.4556+3.8512+5.0342+7.8297)\right]$	M1
	6.814	A1
		(3 marks)

B1 $h = 0.2$ o.e. (including $\frac{5-4}{5}$) seen or implied by sight of e.g. $\frac{0.2}{2}$ or $\frac{1}{10}$ in front of the bracket.
May also be implied by a correct answer if no incorrect working seen. $h = -0.2$ is B0

M1 Correct application of the trapezium rule with their *h* (which may be 1 or *h*).
Look for a correct inner bracket structure $9.2+8.6+2(8.4556+3.8512+5.0342+7.8297)$
condoning slips copying values from the table or the omission of the final brackets on the rhs

e.g. $\frac{1}{2}\times"0.2"(9.2+8.6+2(8.4556+3.8512+5.0342+7.8297$ is M1

but $\frac{1}{2}\times"0.2"\times 9.2+8.6+2(8.4556+3.8512+5.0342+7.8297)$ is M0 unless the brackets are recovered or implied by the correct answer (you may need to check this)

Also allow for a correct method adding individual trapezia using their *h* condoning copying errors but the brackets must be correct (or recovered or implied by later work)

e.g. $\frac{1}{2}\times"0.2"(9.2+8.4556)+\frac{1}{2}\times"0.2"(8.4556+3.8512)+\frac{1}{2}\times"0.2"(3.8512+5.0342)+$
$\frac{1}{2}\times"0.2"(5.0342+7.8297)+\frac{1}{2}\times"0.2"(7.8297+8.6)$

A1 awrt 6.814 isw once a correct answer is seen. Correct answer with no working scores B1M1A1 but if there is evidence of using $h = -0.2$ then maximum awarded is B0M1A0
The A mark cannot be awarded without both B1M1 being awarded on this question.

Question Number	Scheme	Marks
2a	$\left(f\left(\frac{3}{2}\right)=\right)\ 4\left(\frac{3}{2}\right)^3-8\left(\frac{3}{2}\right)^2+5\left(\frac{3}{2}\right)+a=0\Rightarrow a=...$	M1
	$\Rightarrow \frac{27}{2}-18+\frac{15}{2}+a=0\Rightarrow a=-3$ *	A1*
		(2)
b	Example where $2x-3$ is a linear factor: $2x-3\overline{)4x^3-8x^2+5x-3}$ $\quad 2x^2-x+1$ $4x^3-6x^2$ $-2x^2+5x$ $-2x^2+3x$ $+2x-3$ $+2x-3$ 0	M1A1 dM1A1*
	$(-1)^2-4\times2\times1=-7<0\Rightarrow$ no real roots so $x=\frac{3}{2}$ is the only one real root *	
		(4)
		(6 marks)

(a)

M1 Substitutes $x=\frac{3}{2}$ into the expression, sets equal to 0 (may be implied for this mark) and rearranges to find *a*. Condone invisible brackets for this mark only and condone arithmetical slips in their working.

Substituting $x=-\frac{3}{2}$ is M0 and attempts via long division score M0.

A1* $a=-3$ achieved with no errors seen including the omission of brackets.

There must be sight of $x=\frac{3}{2}$ which may be embedded in the expression or $f\left(\frac{3}{2}\right)$ followed by at least one intermediate stage of working/manipulation (it may just be the left hand side of the equation), before proceeding to the given answer. The "$=0$" must be seen somewhere in their working before the given answer.

e.g.

$4\left(\frac{3}{2}\right)^3-8\left(\frac{3}{2}\right)^2+5\left(\frac{3}{2}\right)+a=0\Rightarrow a=-3$ is M1A0

$f\left(\frac{3}{2}\right)=\frac{27}{2}-18+\frac{15}{2}+a=0\Rightarrow a=-3$ is M1A1

Note the trivial case $f\left(\frac{3}{2}\right)=3+a=0\Rightarrow a=-3$ is M1A0 (not enough shown)

(b) Work done in (a) must be made use of in (b) to gain credit.

M1 Attempts to find a quadratic factor of $4x^3-8x^2+5x-3$ using $2x-3$ as a factor

- score for $2x^2\pm x\pm...$ if algebraic division is used or
- score for $2x^2\pm...x\pm1$ if equating coefficients/inspection used.

Alternatively, they may attempt to find a quadratic factor using $x-\frac{3}{2}$ as a factor so

- score for $4x^2 \pm 2x \pm ...$ if algebraic division is used or
- score for $4x^2 \pm ...x \pm 2$ if equating coefficients/inspection used.

A1 $2x^2 - x + 1$ (for $2x-3$ as the linear factor) or $4x^2 - 2x + 2$ (for $x-\frac{3}{2}$ as the linear factor)

dM1 Attempts to show their quadratic factor has no real roots. It is dependent on the previous method mark. Factorisation attempts are M0. Accept via

- an attempt at $b^2 - 4ac$ for their quadratic factor so score for values correctly embedded in $b^2 - 4ac$ for their quadratic
- an attempt to solve their $2x^2 - x + 1$ or $4x^2 - 2x + 2$ using the quadratic formula with values embedded or via a calculator (you must check their roots are correct for their quadratic)
- an attempt to complete the square e.g. $2\left(x \pm \frac{1}{4}\right)^2 \pm ...$

A1* Requires correct factorisation of the cubic, correct calculation for the quadratic, reason and conclusion

For example, after factorising their cubic to e.g. $(2x-3)(2x^2 - x + 1)$ which does not need to be explicitly stated accept e.g.

- the discriminant of $2x^2 - x + 1$ is $-7 < 0$ so only has a root at $x = \frac{3}{2}$. If correct values are embedded which give -7 then this is fine. (For $4x^2 - 2x + 2$ the discriminant is -28)
- $2x^2 - x + 1 = 0 \Rightarrow x = \frac{1}{4} \pm i\frac{\sqrt{7}}{4}$, $(2x-3) = 0 \Rightarrow x = \frac{3}{2}$ so only one real root. (The roots will be the same for $4x^2 - 2x + 2 = 0$)
- $2x^2 - x + 1 = 0 \Rightarrow 2\left(x - \frac{1}{4}\right)^2 + \frac{7}{8} > 0$, hence $x = \frac{3}{2}$ is the only one real root (The completed square form for $4x^2 - 2x + 2$ could be the same or a multiple of it depending on how they have rearranged their inequality)

There must be some reference to the root $x = \frac{3}{2}$ either by stating it or indicating the linear term has a root (e.g. writing "root from here" next to it), but do not accept incorrect statements such as only real root is $(2x-3)$. Condone "solution" for "root"

Do not allow statements such as "Math error" without interpretation of what this means.

Question Number	Scheme	Marks
3a(i)	$r=\sqrt{(8-2)^2+(-3-5)^2}=10$	M1A1
(ii)	$(x-2)^2+(y-5)^2=100$	A1ft
		(3)
b	Gradient between centre and $P = -\frac{4}{3}$	B1
	Perpendicular gradient $=\frac{3}{4}$	M1
	$y+3=\frac{3}{4}(x-8)$	M1
	$3x-4y-36=0$	A1
		(4)
		(7 marks)

(a)(i) **Mark (i) and (ii) together**

M1 Attempts to find the radius. Score for the values embedded in the expression e.g. $\sqrt{(8-2)^2+(-3-5)^2}$ or $\sqrt{(2-8)^2+(5+3)^2}$. They must be attempting to find the difference in the *x* coordinates and the difference in the *y* coordinates.

A1 $(r=)\ 10$ ignore any units ± 10 is A0 Do not accept $\sqrt{100}$ for this mark. isw once a correct answer is seen.

(ii) **Note that if M0 is scored in (a)(i) then this is A0 in (ii)**

A1ft $(x-2)^2+(y-5)^2="100"$ o.e. e.g. $(x-2)^2+(y-5)^2="10^2"$ or $x^2+y^2-4x-10y="71"$ Follow through on their positive single value of *r*. isw once a correct equation is seen.

(b)

B1 Gradient between centre and *P* is $-\frac{4}{3}$ (may be implied by their gradient of the tangent)

M1 Attempts to find the negative reciprocal for their gradient. May be embedded within their equation of the tangent.

M1 Attempts to find the equation of the tangent at *P* using a changed gradient (cannot just be a stated gradient of the tangent which is incorrect and does not follow from any earlier work) and $(8,-3)$

Score for $y+3="\frac{3}{4}"(x-8)$. The coordinates $(8,-3)$ must be correctly placed.

If they use $y=mx+c$ they must proceed as far as $c=...$

A1 $3x-4y-36=0$ o.e. (provided all the coefficients are integers and all terms are on one side of the equation) isw once a correct equation is seen.

Alt (b)
Alternative method using differentiation

B1 $\frac{dy}{dx} = \frac{4-2x}{2y-10}$ o.e. such as $2(x-2)+2(y-5)\frac{dy}{dx} = 0$ or

e.g. $y = \left(100-(x-2)^2\right)^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = -(x-2)\left(100-(x-2)^2\right)^{-\frac{1}{2}}$ (may be implied by $\frac{3}{4}$)

M1 Attempts to find the gradient of the tangent at *P* using their $\frac{dy}{dx}$ and the given coordinate(s).

Do not be concerned with poorly differentiated equations for this mark and just look for the *x* (and possibly *y*) coordinate(s) to be substituted into a differential equation leading to a value for the gradient. Condone sign slips substituting in.

M1 As above in main scheme notes

A1 As above in main scheme notes

Alternative method using formula to find the equation of the tangent at a point on a circle

Using the formula $(x-a)(x_1-a)+(y-b)(y_1-b) = r^2$ with centre (a,b) and point $(x_1,\ y_1)$

B1 $(x-2)(x_1-2)+(y-5)(y_1-5)...$ (may be implied by further work)

M1 Sets equal to their radius: $(x-2)(x_1-2)+(y-5)(y_1-5) = "100"$

M1 Uses the point *P* and sets equal to their radius: $(x-2)(8-2)+(y-5)(-3-5)... = "100"$

A1 $3x-4y-36 = 0$ oe (provided all the coefficients are integers and all terms are on one side of the equation)

Question Number	Scheme	Marks
4a	3^5 or 243	B1
		(1)
bi	$(B=)5\times3^4p\ (=405p)$ $\quad$ $(D=)10\times3^2p^3\ (=90p^3)$	M1A1
	$B=18D \Rightarrow= 405p=18\times90p^3 \Rightarrow p^2=\frac{1}{4}\Rightarrow p=-\frac{1}{2}$	M1A1
ii	$(C=)\ {}^5C_2\times3^3\times\left(-\frac{1}{2}\right)^2=\frac{135}{2}$	M1A1
		(6)
		(7 marks)

(a) **Mark (a) and (b) together**

B1 3^5 or 243 seen. Do not award if it is outside the bracket as $3^5\left(1+\frac{px}{3}\right)^5$, but allow if some of the terms of the binomial expansion are found and 243 is the constant term.
e.g. $243+405px+...$ Do not accept e.g. ${}^5C_0\times243\times(px)^0$ for this mark.

(b)(i)

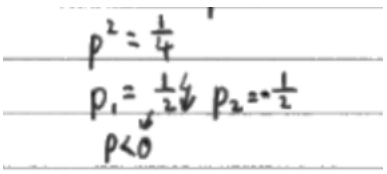
M1 $(B=)5\times3^4p\ (=405p)$ or $(D=)10\times3^2p^3\ (=90p^3)$ (simplified or unsimplified including unprocessed indices).
The coefficients of *B* or *D* may be embedded within the binomial expansion such as $...+5\times3^4px+...+10\times3^2(px)^3$. Also allow e.g. $\binom{5}{1}3^4p$ or $\binom{5}{3}3^2p^3$ or ${}^5C_1 3^4p$ or ${}^5C_3 3^2p^3$

A1 $(B=)5\times3^4p\ (=405p)$ and $(D=)10\times3^2p^3\ (=90p^3)$ (simplified or unsimplified) Allow this mark if the coefficients have not been isolated from *x* and x^3, but the brackets around (px) and $(px)^3$ must be correctly removed. Binomial notation such as ${}^5C_1$ or ${}^5C_3$ must have been evaluated.

M1 Uses $"B"=18"D"$ to form a cubic equation in *p* and attempts to take out a factor of *p* or divide by *p* leading to $p^2=...$ (or may be implied by their value of *p*). $"B"="D"$ is M0
Condone equations involving *x* and x^3 as long as they are removed as they proceed to $p^2=...$
Note that equations may have been simplified before they are formed by cancelling factors e.g. 3^2, 3, 5 or *p* so look carefully at equations which are acceptable such as $5\times3^2p=180p^3$ or $9=36p^2\Rightarrow p^2=...$ (condone if negative)

Note $405p=90p^3\Rightarrow p=\pm\frac{3\sqrt{2}}{2}$ **scores M1A1M0A0 in (b)(i)** (did not use $"B"=18"D"$)
They can proceed in (b)(ii) to score M1A0.

A1 $p=-\frac{1}{2}$ only following correct coefficients for *B* and *D* (the positive root and $p=0$ must be rejected if found / a clear choice of $p=-\frac{1}{2}$) Watch out for notation rejecting the positive root such as:



Can only be scored provided all previous marks have been awarded.

Note if the coefficients of *B* and *D* are incorrect leading to $p=-\frac{1}{2}$ then this is max M0A0M1A0 in (b) and M1A0 in (c)

Alternative method (b)(i)

If the expansion is written as $243\left(1+5\left(\frac{px}{3}\right)+\frac{5\times4}{2!}\left(\frac{px}{3}\right)^2+\frac{5\times4\times3}{3!}\left(\frac{px}{3}\right)^3\right)$ then 243 is not required to find *p* as this will cancel from both sides when setting $"B"=18"D"$.

M1 $(B=)\ (243\times)5\left(\frac{p}{3}\right)$ or $(D=)(243\times)\frac{5\times4\times3}{3!}\left(\frac{p}{3}\right)^3$ (unsimplified with or without the 243)

A1 $(B=)\ (243\times)5\left(\frac{p}{3}\right)$ and $(D=)(243\times)\frac{5\times4\times3}{3!}\left(\frac{p}{3}\right)^3$ (unsimplified either both with or both without the 243 included). Allow this mark if the coefficients have not been isolated from *x* and x^3, but the brackets around $\left(\frac{px}{3}\right)$ and $\left(\frac{px}{3}\right)^3$ must be correctly removed. Any binomial notation would now have to be evaluated as in the main scheme notes.

M1 As above in main scheme notes

A1 As above in main scheme notes

(ii)

M1 Uses their value of p^2, p or $|p|$ and either attempts ${}^5C_2\times3^3p^2$ to find a value for *C*, or attempts to find ${}^5C_2\times3^3p^2x^2$ and then proceeds to identify the value for *C*.

Condone values for *p* where *x* had not been removed from (i) e.g. $\pm\frac{1}{2}x$ being substituted in provided a value without *x* is identified/extracted in (ii)

Condone a slip in calculating ${}^5C_2$ and allow this mark if they substitute both values of *p* into the expression and find two values for *C*.

The method mark may be implied by the value found using their *p*

A1 $\frac{135}{2}$ o.e. e.g. 67.5 or $67\frac{1}{2}$ or $\frac{270}{4}$ following a correctly found $p=\pm\frac{1}{2}$ or $p^2=\frac{1}{4}$

Condone where both values of *p* are used provided they both give the correct answer.

Do not accept e.g. $\frac{135}{2}x^2$ unless the coefficient is clearly identified

Question Number	Scheme	Marks
5	$\log_2 16x + \log_2(x+1) = 3 + \log_2(x+6)$	
	$\log_2 a = b \Rightarrow 2^b = a$	B1
	$\log_2 16x(x+1) = \log_2 8(x+6)$	M1
	$2x^2 + x - 6 = 0$	A1
	$(2x-3)(x+2) = 0$	dM1
	$x = \frac{3}{2}$ only	A1cso
		(5 marks)

Note a correct answer with no working is 0 marks

B1 Correct use of $\log_2 a = b \Rightarrow 2^b = a$ This will usually result from either $\log_2 8 = 3$ or $\log_2 16 = 4$ being stated or seen applied.

e.g. $\log_2\left(\frac{16x(x+1)}{x+6}\right) = 3 \Rightarrow \frac{16x(x+1)}{x+6} = 8$

May be implied by e.g. $\log_2 16x(x+1) = \log_2 8(x+6)$ or $\log_2\left(\frac{x(x+1)}{x+6}\right) = -1$ o.e.

M1 Applies the addition (or subtraction) laws of logs at least once correctly. Condone invisible brackets. e.g. $\log_2 16x^2 + 16x$

This mark can be scored for expressions where the law has been applied correctly and does not need to be a full equation e.g. $\log_2\left(\frac{x+6}{x+1}\right)$ scores M1. Do not withhold this mark if they subsequently apply a law incorrectly.

e.g. $\log_2 16x(x+1) = 3 + \log_2 x + \log_2 6$ still scores M1

Also allow the mark to be scored despite an error dealing with the 3 when writing it as a log

e.g. $3 + \log_2(x+6) = \log_2 6 + \log_2(x+6) = \log_2 6(x+6)$

A1 $2x^2 + x - 6 = 0$ or equivalent 3TQ (quite often $16x^2 + 8x - 48 = 0$) Terms must be collected but do not need to be collected on the same side. Condone the omission of = 0 . Can only be scored from correct working.

dM1 Attempts to solve their 3TQ via any valid method including via a calculator (you may need to check this). Condone complex roots. It is dependent on the previous method mark.

A1cso $\frac{3}{2}$ o.e. only (-2 must be rejected if found)

This mark can only be scored if a correct quadratic is achieved (following correct log work)

Question Number	Scheme	Marks
6a	$\dfrac{k}{2k-15}=\dfrac{k+4}{k}\Rightarrow k^2=2k^2+8k-15k-60\Rightarrow k^2-7k-60=0$ *	M1A1*
		(2)
b	$k=12$	B1
	$\Rightarrow \dfrac{"12"}{2\times"12"-15}\ \left(=\dfrac{4}{3}\right)$	M1
	e.g. $("12"+4)\times\dfrac{4}{3}=...$ or $(2\times"12"-15)\times\left("\dfrac{4}{3}"\right)^3=...$	M1
	$=21300$	A1
		(4)
c	e.g. $\dfrac{9\left(1-\left(\dfrac{4}{3}\right)^N\right)}{1-\dfrac{4}{3}}>3000\Rightarrow\left(\dfrac{4}{3}\right)^N>\dfrac{1009}{9}$	M1
	$\log\left(\dfrac{4}{3}\right)^N>\log\left(\dfrac{1009}{9}\right)\Rightarrow N>\dfrac{\log\left(\dfrac{1009}{9}\right)}{\log\left(\dfrac{4}{3}\right)}$	dM1
	$N>16.405...\Rightarrow N=17$	A1
		(3)
		(9 marks)

(a)

M1 Forms a correct equation linking the three terms and attempts to rearrange to the given quadratic (it cannot be awarded for just proceeding in one step from the starting equation to the given answer and usually will involve attempting to multiply out brackets or dealing with any fractions). Must proceed as far as a quadratic with terms collected.
Condone slips in their rearrangement and invisible brackets.
Possible starting equations will involve using the *n*th term formula or the sum of a geometric series. The ones below are not exhaustive.

$\dfrac{k}{2k-15}=\dfrac{k+4}{k}$ or $k^2=(k+4)(2k-15)$ $\left((u_2)^2=u_1\times u_3\right)$ or $(2k-15)\left(\dfrac{k+4}{k}\right)=k$ or

$k\left(\dfrac{k}{2k-15}\right)=k+4$ or $2k-15+k+k+4=\dfrac{(2k-15)\left(1-\left(\dfrac{k}{2k-15}\right)^3\right)}{1-\dfrac{k}{2k-15}}$ (sum of 3 terms)

A1* Rearranges to achieve $k^2-7k-60=0$ with no errors seen including brackets. There must be at least some intermediate working (e.g. brackets multiplied out or multiplying to remove any fractions) between their starting equation and the given answer.

(b) **Note a candidate who uses *k* as *r* can only score maximum B1 in (b) and no marks in (c)**

B1 12 (ignore -5) seen or used in (b) (may be implied by the value of the second term)

M1 Substitutes their 12 (must be positive) into the expressions for two of the terms and attempts to find a value for *r*. Condone arithmetical slips but they the division the correct way round.

M1 Attempts to find the 4th term using their positive k and their positive r eg $("12"+4)\times"\frac{4}{3}"=...$

(may be implied by awrt 21.3). Alternatively, they may find the first term a and use this with their r to find the 4th term. Condone slips in finding a

Condone r to be rounded from their earlier work and condone missing brackets but not incorrectly placed brackets.

A1 21300 or 21330 or 21333 only or their equivalences e.g. 21.3 thousand

(c) **Typically, candidates will work in base 10, but other bases such as their r is acceptable**

M1 Uses their $a="9"$ or $a="9000"$ and their positive $r="\frac{4}{3}"$ in the sum of a geometric formula $\Rightarrow$

$\frac{"9"\left(1-\left("\frac{4}{3}"\right)^N\right)}{1-"\frac{4}{3}"}$....3... (may be = or any inequality in between) and proceeds to $A\left("\frac{4}{3}"\right)^N...B$

(condone $A\times B$ to be negative), where A could be 1 and B could be unsimplified. Do not be concerned with the number of 0s after the 3.

Do not be concerned by the mechanics of their rearrangement and may be implied by further work if logarithms are used correctly. Condone r to be rounded from their earlier work and condone missing brackets but not incorrectly placed brackets.

dM1 Attempts to find N using logarithms correctly. Do not be concerned with the use of equals or the direction of any inequality used for this mark. May be implied by a correct expression (not a value) for N. It is dependent on the previous method mark.

This mark can only be scored if $A\times B>0$ for their $A\left("\frac{4}{3}"\right)^N...B$

A1 17 cso (if an incorrect inequality sign is used at some point in their working then withhold this final mark) This mark can only be scored provided there are **no arithmetical errors** and **correct log work** is seen as part of their solution. Do not withhold the mark for invisible brackets around their $\left(\frac{4}{3}\right)^N$. Condone if r is rounded from $\frac{4}{3}$. If a value for N is found before deducing $N=17$ then it must be 16.4 or better. 17 with no working seen is 0 marks.

Note e.g. $N>\log_{\frac{4}{3}}\left(\frac{991}{9}\right)\Rightarrow N=17$ is A0 (arithmetical slip combining $1+\frac{1000}{9}$)

$\frac{9\left(1-\left(\frac{4}{3}\right)^N\right)}{1-\frac{4}{3}}>3000\Rightarrow\left(\frac{4}{3}\right)^N>\frac{1009}{9}\Rightarrow N=17$ scores M1dM0A0 (insufficient working)

$\frac{9\left(1-\left(\frac{4}{3}\right)^N\right)}{1-\frac{4}{3}}<3000\Rightarrow N<\frac{\log\left(\frac{1009}{9}\right)}{\log\left(\frac{4}{3}\right)}\Rightarrow N=17$ scores M1dM1A0 (inequality sign errors)

$\frac{9000\left(1-\left(\frac{4}{3}\right)^N\right)}{1-\frac{4}{3}}>3000000\Rightarrow N>\log_{\frac{4}{3}}\left(\frac{1009}{9}\right)\Rightarrow N=17$ scores M1dM1A1 (implied M marks)

Note: Methods relying on trial and improvement, or the equation solver score maximum M1dM0A0

Question Number	Scheme	Marks
7a	$H = t^{\frac{1}{2}} + \frac{3t^{\frac{3}{2}}}{10} - \frac{t^{\frac{5}{2}}}{20} + 17 \Rightarrow \left(\frac{\mathrm{d}H}{\mathrm{d}t} =\right) \frac{1}{2}t^{-\frac{1}{2}} + \frac{9}{20}t^{\frac{1}{2}} - \frac{1}{8}t^{\frac{3}{2}}$	M1A1A1
	e.g. $\frac{1}{2}t^{-\frac{1}{2}} + \frac{9}{20}t^{\frac{1}{2}} - \frac{1}{8}t^{\frac{3}{2}} = 0 \Rightarrow \frac{1}{2} + \frac{9}{20}t - \frac{1}{8}t^2 = 0 \ldots \Rightarrow 5\alpha^2 - 18\alpha - 20 = 0$ *	dM1A1*
		(5)
b	$\alpha = \frac{9+\sqrt{181}}{5} = \text{awrt } 4.491$	B1
		(1)
c	$\left(\frac{\mathrm{d}^2H}{\mathrm{d}t^2} =\right) -\frac{1}{4}t^{-\frac{3}{2}} + \frac{9}{40}t^{-\frac{1}{2}} - \frac{3}{16}t^{\frac{1}{2}} \Rightarrow -\frac{("4.49")^{-\frac{3}{2}}}{4} + \frac{9("4.49")^{-\frac{1}{2}}}{40} - \frac{3("4.49")^{\frac{1}{2}}}{16}$	M1
	$\frac{\mathrm{d}^2H}{\mathrm{d}t^2} = (-0.3\ldots) < 0 \Rightarrow \max$ *	A1*
		(2)
		(8 marks)

(a) **If they change *t* to α before differentiating then score maximum M1A1A0dM1A0**

M1 Multiplies out and attempts to differentiate. Award for one correct index from correct working (may be implied if they multiply out and differentiate at the same time) $t^{\frac{3}{2}}$ or $t^{\frac{1}{2}}$ or $t^{-\frac{1}{2}}$ (condone if these are $\alpha^{\frac{3}{2}}$ or $\alpha^{\frac{1}{2}}$ or $\alpha^{-\frac{1}{2}}$ or any other variable) The indices do not need to be processed for this mark.
e.g. $t^{\frac{5}{2}-1}$
Alternatively, they may attempt the product rule so look for a correct general expression such as $\left(\frac{\mathrm{d}H}{\mathrm{d}t} =\right) \ldots t^{-\frac{1}{2}}(20+6t-t^2) + \ldots t^{\frac{1}{2}}(A+Bt)$ (condone if in terms of α or another variable instead)

A1 One of $\frac{1}{2}t^{-\frac{1}{2}}$, $\frac{9}{20}t^{\frac{1}{2}}$, $-\frac{1}{8}t^{\frac{3}{2}}$ (simplified or unsimplified) via the main scheme
If they differentiate using the product rule then this mark can only be awarded for one of $\frac{1}{40}t^{-\frac{1}{2}}(20+6t-t^2) + \ldots t^{\frac{1}{2}}(A+Bt)$ or $\ldots t^{-\frac{1}{2}}(20+6t-t^2) + \frac{1}{20}t^{\frac{1}{2}}(6-2t)$ (unsimplified).
In both cases the indices must be processed. Condone if in terms of α

A1 $\left(\frac{\mathrm{d}H}{\mathrm{d}t} =\right) \frac{1}{2}t^{-\frac{1}{2}} + \frac{9}{20}t^{\frac{1}{2}} - \frac{1}{8}t^{\frac{3}{2}}$ or equivalent e.g. $\left(\frac{\mathrm{d}H}{\mathrm{d}t} =\right) \frac{1}{40}t^{-\frac{1}{2}}\left(20+18t-5t^2\right)$ which may be unsimplified. Also allow
e.g. $\left(\frac{\mathrm{d}H}{\mathrm{d}t} =\right) \frac{1}{40}t^{-\frac{1}{2}}(20+6t-t^2) + \frac{1}{20}t^{\frac{1}{2}}(6-2t)$ (via the product rule)

dM1 Sets their derivative of the form $\ldots t^{-\frac{1}{2}} \pm \ldots t^{\frac{1}{2}} \pm \ldots t^{\frac{3}{2}} = 0$ (may be implied) and proceeds via a correct method to a 3TQ in *t* or α (or any other variable) where the powers and the coefficients of the terms are integers. Condone sign slips only. It is dependent on the previous method mark.
Proceeding directly to the given answer is M0, unless they state how they have proceeded from the derivative directly to the given answer e.g. set $t = \alpha$ **and** $\times -40t^{\frac{1}{2}}$

Derivatives which are already factorised before being set = 0 and have the quadratic factor $20+18t-5t^2$ can score this mark for

e.g. $\left(\frac{\mathrm{d}H}{\mathrm{d}t}=\right)\frac{1}{40}t^{-\frac{1}{2}}\left("20+18t-5t^2"\right)=0\Rightarrow "5t^2-18t-20"=0$

A1* Achieves $5\alpha^2-18\alpha-20=0$ with no errors seen and all previous marks scored. Must be in terms of α (do not be concerned if it looks like a) . The $=0$ must have been seen before achieving the given answer.

Do not be concerned with the labelling of the derivative if seen e.g. $\frac{\mathrm{d}y}{\mathrm{d}x}$ instead

Do not penalise invisible brackets as long as they are recovered and the intention is clear through their subsequent lines of working.

Alternative method: They may attempt to multiply by e.g. 20 or take out a factor and then differentiate. This can score full marks, provided for A1* they explain at some point that this does not affect the given answer. You will need to check their terms are correct for the first A mark and withhold the A marks if e.g. they do not multiply all terms including the +17 by 20

(b) Mark (b) and (c) together

B1 $\alpha=$awrt 4.491 only. Accept the exact answer. If both roots are stated then awrt 4.491 must be the only one used within their $\frac{\mathrm{d}^2H}{\mathrm{d}t^2}$, or if both values are used then the other is rejected. If awrt 4.491 is seen then allow for it to be subsequently rounded to 2 or 3sf when used as evidence of selecting awrt 4.491

(c)

M1 Attempts to differentiate their $\frac{\mathrm{d}H}{\mathrm{d}t}$ to achieve a second derivative of the form $...t^{-\frac{3}{2}}+...t^{-\frac{1}{2}}+...t^{\frac{1}{2}}$ (may be in terms of α or another variable) and either attempts to substitute in their value of α which must be between 0 and 7 or considers the sign of their second derivative. Condone their α to have been subsequently rounded before substituted in

May be seen as $\frac{1}{40}t^{-\frac{1}{2}}\left(20+18t-5t^2\right)\rightarrow-\frac{1}{80}t^{-\frac{3}{2}}\left(20-18t+15t^2\right)$

If differentiation in part (a) is via the product rule then look for an attempt to apply the product rule on their $\left(\frac{\mathrm{d}H}{\mathrm{d}t}=\right)...t^{-\frac{1}{2}}(20+6t-t^2)+...t^{\frac{1}{2}}(A+Bt)$ leading to

$...t^{-\frac{3}{2}}(20+6t-t^2)+...t^{-\frac{1}{2}}(C+Dt)+...t^{\frac{1}{2}}$

Alternatively, attempts to show that the second derivative is always negative. e.g. attempts to complete the square on $20-18t+15t^2$ and considers its sign.

A1* $\frac{\mathrm{d}^2H}{\mathrm{d}t^2}\ (=-0.3)<0\Rightarrow$ max when $\alpha=$awrt 4.491. If evaluated, it must be -0.3 or better ($-0.3174...$). The second derivative must be correct but condone in terms of α

In the alternative method look for correct working and valid argument explaining that eg $20-18t+15t^2$ is always greater than zero so $-\frac{1}{80}t^{-\frac{3}{2}}\left(20-18t+15t^2\right)$ is always negative for any value of t

Condone poor phrasing as part of the explanation e.g. "$t=4.491$ is a maximum" instead of "$t=4.491$ is the value at which H is at a maximum"

Condone poor notation for $\frac{\mathrm{d}^2H}{\mathrm{d}t^2}$ and condone e.g. $y"$

<table>
<tr><th>Question Number</th><th>Scheme</th><th>Marks</th></tr>
<tr><td>8(i)</td><td>Eg $7^2+11^2=170 \Rightarrow 170$ is a multiple of 10 so the statement is untrue *</td><td>M1A1*</td></tr>
<tr><td></td><td></td><td>(2)</td></tr>
<tr><td>(ii)</td><td>Check first if they have multiplied the inequality e.g. by 4 to give $4 < 4x^2 - xy < 60$
<table>
<tr><th>x</th><th>y</th><th>$x^2 - \frac{xy}{4}$ or $4x^2 - xy$</th></tr>
<tr><td>2</td><td>2</td><td>3 12</td></tr>
<tr><td>2</td><td>4</td><td>2 8</td></tr>
<tr><td>4</td><td>2</td><td>14 56</td></tr>
<tr><td>4</td><td>4</td><td>12 48</td></tr>
</table>
Concludes that $1 < x^2 - \frac{xy}{4} < 15$ for all x and y that are positive even integers less than 6 *</td><td>M1A1

A1*</td></tr>
<tr><td></td><td></td><td>(3)</td></tr>
<tr><td></td><td></td><td>(5 marks)</td></tr>
</table>

(i)

M1 Attempts to find a^2+b^2 using two consecutive prime numbers a and b. It does not matter whether this combination of prime numbers results in a multiple of 10 to score M1. Condone slips in their evaluation of the sum of the squares of these two numbers. If a candidate has several combinations, you only need to look for one calculation using two consecutive prime numbers.
Note $1^2+2^2=...$ as the only calculation is M0A0

A1* Correctly:

- evaluates the sum of two consecutive prime numbers squared
- either
  - makes a comment that the answer is a multiple of 10
  - makes a comment that 10 is a factor of their answer
  - makes a comment that their answer is divisible by 10 (do not accept can be divided by 10)
  - shows that the answer is a multiple of 10 (such as splitting the number into two factors, one of which is 10, or showing the number is divisible by 10 e.g. $\frac{170}{10}=17$)
- concludes not true o.e. (condone e.g. "not correct", "not always true")

If a candidate has several combinations, you do not need to check all of them. Just look for one which would lead to correct counter example.

Below are a list of common combinations which provide the required counter example but there will be others

- $7^2+11^2=170$
- $11^2+13^2=290$
- $17^2+19^2=650$
- $19^2+23^2=890$
- $23^2+29^2=1370$

(ii)

M1 Attempts at least two valid combinations of x and y and evaluates $x^2 - \frac{xy}{4}$ condone slips in the evaluation of the combinations.
Alternatively, attempts at least two valid combinations of x and y and evaluates $4x^2 - xy$

A1 All four valid combinations of x and y correctly evaluated for $x^2 - \frac{xy}{4}$ (or in the alternative method $4x^2 - xy$)

A1* A minimal conclusion that $1 < x^2 - \frac{xy}{4} < 15$ (or condone $4 < 4x^2 - xy < 60$) for all x and y that are positive even integers less than 6.
e.g. “hence statement is true”, “they are all between 1 and 15” (or 4 and 60 in the alternative), “proven”, “QED” or they may have a preamble which can be concluded with a tick or similar.

Question Number	Scheme	Marks
9a	$3\cos\theta(\tan\theta\sin\theta+3)=11-5\cos\theta$ $3\sin^2\theta+9\cos\theta=11-5\cos\theta$ or $3\cos\theta\left(\frac{\sin\theta}{\cos\theta}\sin\theta+3\right)=11-5\cos\theta$ $3(1-\cos^2\theta)+9\cos\theta=11-5\cos\theta$ $3\cos^2\theta-14\cos\theta+8=0$ *	M1 dM1 A1*
		(3)
b	$\cos 2x=\frac{2}{3}$ $x=\frac{\cos^{-1}\left(\frac{2}{3}\right)}{2}=...$ $x=$ awrt 24.1, awrt 155.9, awrt 204.1, awrt 335.9	B1 M1 A1A1
		(4)
		(7 marks)

(a)

M1 Substitutes or uses $\tan\theta=\frac{\sin\theta}{\cos\theta}$ to achieve an equation in sine and cosine only.
May be in another variable and condone if there is a mix of variables in the same equation for this mark.

dM1 Attempts to use $\pm\sin^2\theta\pm\cos^2\theta=\pm1$ to achieve an equation in cosine only. It is dependent on the previous method mark. Condone slips in their manipulation of the equation.
May be in another variable and condone if there is a mix of variables in the same equation for this mark.

A1* Achieves $3\cos^2\theta-14\cos\theta+8=0$ with no errors seen including brackets. Withhold this mark for poor notation used such as $3\cos\theta^2-14\cos\theta+8=0$
Allow a candidate to work consistently in one variable and then change to θ but withhold this final mark if there is a mixture of variables within the same equation/line of working.

(b) **Note that answers only scores 0 marks. May work in any variable and do not be concerned as to whether they are writing e.g. *x* or 2*x* in their working**

B1 $(\cos...=)\ \frac{2}{3}$ (ignore any reference to 4)

M1 Solves using the correct order of operations to find at least one value for *x*. You may need to check this on your calculator. May be implied by a correct value for $\cos 2x="\frac{2}{3}"$

A1 Two of awrt 24, awrt 156, awrt 204, awrt 336 . (Condone in radians two of awrt 0.42, awrt 2.7, awrt 3.6, awrt 5.9)

A1 awrt 24.1, awrt 155.9, awrt 204.1, awrt 335.9 and no others in the range
Minimum acceptable to be able to score full marks:
e.g. $\cos...=\frac{2}{3}\Rightarrow$ *answers* or $(...=)\ \cos^{-1}\left(\frac{2}{3}\right)\Rightarrow$ *answers*

Question Number	Scheme	Marks
10a	$\dfrac{(x-k)^2}{\sqrt{x}} = \dfrac{x^2-2kx+k^2}{x^{\frac{1}{2}}} = \dfrac{x^2}{x^{\frac{1}{2}}} - \dfrac{2kx}{x^{\frac{1}{2}}} + \dfrac{k^2}{x^{\frac{1}{2}}} = x^{\frac{3}{2}} - 2kx^{\frac{1}{2}} + k^2x^{-\frac{1}{2}}$	M1
	$\int_1^{16} x^{\frac{3}{2}} - 2kx^{\frac{1}{2}} + k^2x^{-\frac{1}{2}}\,\mathrm{d}x = \left[\dfrac{2}{5}x^{\frac{5}{2}} - \dfrac{4}{3}kx^{\frac{3}{2}} + 2k^2x^{\frac{1}{2}}\right]_1^{16}$	M1A1
	$\dfrac{2}{5}(16)^{\frac{5}{2}} - \dfrac{4}{3}k(16)^{\frac{3}{2}} + 2k^2(16)^{\frac{1}{2}} - \dfrac{2}{5} + \dfrac{4}{3}k - 2k^2 = 6k^2 - 84k + \dfrac{2046}{5}$	dM1A1
		(5)
b	$9 = \dfrac{(1-k)^2}{\sqrt{1}} \Rightarrow 9 = (1-k)^2$	M1
	$k = 4$ only *	A1*
		(2)
c	$q = 36$	B1
	$\dfrac{1}{2}(9+"36")\times 15 - \left("6"(4)^2 - "84"(4) + \dfrac{2046}{5}\right) = \dfrac{1683}{10}$	M1A1
		(3)
		(10 marks)

(a)

M1 Attempts to multiply out the numerator and split the fraction into separate terms. Score for one term with a correct index (which must be processed). Any attempts via substitution e.g. setting $u = \sqrt{x}$ send to review. Condone poor attempts at multiplying out the brackets such that $(x-k)^2 \Rightarrow x^2 \pm k^2$

M1 Attempts to raise the power (which must be a fraction or decimal) by one on one of their terms. (The index does not need to be processed).

A1 $\dfrac{2}{5}x^{\frac{5}{2}} - \dfrac{4}{3}kx^{\frac{3}{2}} + 2k^2x^{\frac{1}{2}}$ or unsimplified equivalent. Indices must be processed. Ignore any spurious notation around the expression. May be with or without $+c$

dM1 Substitutes in 16 and 1 for *x* and subtracts either way round. The values embedded are sufficient and condone invisible brackets. It is dependent on the previous method mark.

A1 $6k^2 - 84k + \dfrac{2046}{5}$ o.e. e.g. $6k^2 - 84k + 409.2$ isw after a correct answer is seen, but withhold this mark if there is spurious notation such as $\int$ or $\mathrm{d}x$ at either the start or end of the answer.

(b)

M1 Substitutes the coordinates of *A* into the equation for *C* or, alternatively, substitutes in the coordinates of *A* and $k = 4$ into the equation for *C*.

A1* Solves either:

- $9 = (1-k)^2 \Rightarrow k = ...$
- $k^2 - 2k - 8 = 0$ with terms collected to a 3TQ via any allowable method including via a calculator.

With either method they must proceed to $k = 4$ only with no errors seen, including invisible brackets. If -2 is found it must be rejected or 4 clearly selected. If they use $k = 4$ in their solution, then there must be a minimal conclusion.

(c)

B1 $q = 36$ seen (may be in (b) or on the diagram) or implied for example by a correct area of a triangle or trapezium.

M1 Attempts to find the area of *R* using their *q* and **their answer to part (a)**. Condone arithmetical slips and do not be concerned with poor notation for this mark. Must proceed to find a value for the area but condone subtracting areas the wrong way round which may result in a negative area.

Possible methods include:

e.g. Line – curve: $\int_1^{16} \frac{9}{5}x + \frac{36}{5}\,\mathrm{d}x$ – part (a) with $k = 4$

e.g. Area of trapezium ($= 337.5$) – part (a) with $k = 4$

Note: the correct values if the trapezium is split into a rectangle and a triangle are 135 and 202.5, respectively.

For evidence of use of part (a), look for $k = 4$ to be substituted into their part (a) answer, or may be implied by a correct value for their $6k^2 - 84k + \frac{2046}{5}$ with $k = 4$

Condone $\int_1^{16} \frac{(x-k)^2}{\sqrt{x}}\,\mathrm{d}x = 169.2$ provided their part (a) is correct

A1 $\frac{1683}{10}$ oe (ignore units) Condone spurious notation.

Withhold this mark if their method results in a negative area but they just omit the negative sign. They would need to indicate area is positive for e.g. $A = ... - .... = -\frac{1683}{10}$ so $A = \frac{1683}{10}$

Question Number	Scheme	Marks
11a	$u_2 = b - 3a$ $u_3 = b - a(b-3a) \quad \left(= b - ab + 3a^2\right)$	B1 B1
		(2)
b	$3 + b - 3a + b - a(b-3a) = 153$ oe $3 + (a+9) - 3a + (a+9) - a((a+9) - 3a) = 153 \Rightarrow 2a^2 - 10a - 132 = 0$ $\Rightarrow a^2 - 5a - 66 = 0$ *	M1 dM1A1*
		(3)
c	$a = -6$ $b = 9 - 6 = 3 \Rightarrow u_2 = 3 - 3(-6) = 21$ or $u_2 = 9 - 2a = 9 - 2\times -6 = 21$	B1 M1A1
		(3)
		(8 marks)

(a) **Check next to the question. If there is a contradiction between the answer next to the question and the answer in the main body of the work then the answer in the main body of the work takes precedence.**

B1 $(u_2 =)\ b - 3a$ oe

B1 $(u_3 =)\ b - a(b-3a)$ oe isw

(b)

M1 Attempts to add 3, their u_2 and their u_3 and sets equal to 153. Condone slips in their copying of their expressions for u_2 and u_3. Invisible brackets may be implied by further work.
May be in terms of a or b only if they substitute in $b = a + 9$ at the same time.
e.g. $3 + a + 9 - 3a + a + 9 - a(a + 9 - 3a) = 153$

dM1 Attempts to substitute $b = a + 9$ into their equation and then attempts to collect terms to achieve a 3TQ in a (condone the omission of = 0). The three terms do not all need to be on the same side of the equation. It is dependent on them having a u_3 term which would lead to an a^2 term. Do not be too concerned by the mechanics of their rearrangement for this mark. It is dependent on the previous method mark.

A1* Achieves the given answer with no arithmetical errors seen. Condone recovery of missing brackets, provided the recovery is before the final answer. Must see at least one intermediate stage of working following an equation in a only, before proceeding to the given quadratic equation.

(c)

B1 $a = -6$ seen or used in (c). Ignore the positive root for this mark.

M1 Attempts to substitute their negative root into $b = a + 9$ to find a value for b and then uses these in their expression for u_2 to find a value for u_2
Alternatively, attempts to substitute both their negative root and $b = a + 9$ into their expression for u_2 and proceeds to find a value for u_2
Ignore working relating to where they repeat the calculations to find u_2 using their positive root
May be implied by their answer (you may need to check this)

Note: For candidates who have two roots of the same sign then this mark can be awarded for using their smaller value (i.e. most negative/least positive) and proceeding to find a value for u_2

A1 21 only cao (if two answers are reached they must select 21 or reject the other answer)
Correct answer on its own scores full marks.

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